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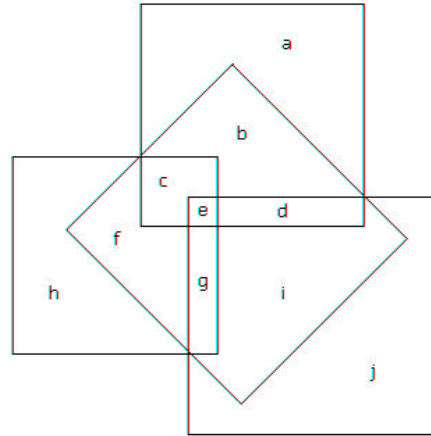
S-48 Solution:

Label the squares as shown in the diagram.
Let S be the sum of each square. Then

$$\begin{aligned} a + b + c + d + e &= S \\ d + g + i + j + e &= S \\ c + f + e + g + h &= S \\ b + c + d + e + f + g + i &= S \end{aligned}$$

Equating each of the first 3 equations with the last one to get

$$\begin{aligned} a &= f + g + i \\ j &= b + c + f \\ h &= b + d + i \end{aligned}$$



Only 6, 7, 8, 9 and 10 can be decomposed into the sum of 3 digits. Namely,

$$\begin{array}{lllll} 6=1+2+3 & 7=1+2+4 & 8=1+2+5 & 9=1+2+6 & 10=1+2+7 \\ & & 8=1+3+4 & 9=1+3+5 & 10=1+3+6 \\ & & & 9=2+3+4 & 10=1+4+5 \\ & & & & 10=2+3+5 \end{array}$$

To get distinct digits for each letter, all we have to do is to pick three equalities each from a different column and row. There are only two possibilities:

$$\begin{array}{ll} 8=1+2+5 & 8=1+3+4 \\ 9=2+3+4 & 9=1+2+6 \\ 10=1+3+6 & 10=2+3+5 \end{array}$$

Therefore the digit that goes into the ? spot is 7.