

1123. Proposed by Mike Pinter, Belmont University, Nashville, TN

This problem is in honor of the 300th birthday of Benjamin Franklin. Consider the base 9 cryptarithm $K I T E + K E Y = S H O C K$. Find a solution that minimize the $S H O C K$.

Solution by **Rex H. Wu**, Brooklyn, NY.

$$\begin{array}{r} K I T E \\ + \quad K E Y \\ \hline S H O C K \end{array}$$

On the 9^3 column, K get a 1 from the 9^2 column and 1 is carried to the 9^4 column. Therefore, $S = 1, H = 0$ and $K = 8$.

On the 9^0 column, $E + Y = K = 8$. Of the remaining digits, only $2 + 6 = 8$ or $3 + 5 = 8$.

To minimize the $SHOCK$, let $O = 2$. Since I cannot be 2, this means $I = 3$. But then the 9^0 column cannot be satisfied.

Let $O = 3$. Again, I cannot be 2 since we have to leave 2 to the 9^0 column. Therefore $I = 4$.

$I = 4$ implies the 9^1 column cannot carry a 1 to the 9^2 column. We are left with the digits 2, 5, 6 and 7. 2 and 6 have to be used for the 9^0 column. $E = 6$ leave no solution for the 9^1 column. Therefore, $E = 2, Y = 6, T = 5$ and $C = 7$.

$$K I T E + K E Y = 8 4 5 2 + 8 2 6 = 1 0 3 7 8 = S H O C K.$$

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