

ELEMENTARY TRIGONOMETRY EQUATIONS – WORKSHEET

COURSE/LEVEL

NSW Secondary High School Year 11 Preliminary Mathematics.

Syllabus reference: 5.1 – 5.2.

1. Solve the following equations for θ if $0^\circ \leq \theta < 360^\circ$.

I

(a) $\sin \theta = 0$

(b) $\sin \theta = 1$

(c) $\cos \theta = \frac{1}{\sqrt{2}}$

(d) $\sin \theta = -1$

(e) $\tan \theta = -\sqrt{3}$

(f) $2 \sin \theta = 1$

(g) $\sin \theta = \cos \theta$

(h) $\sin^2 \theta = \frac{1}{2}$

(i) $\tan^2 \theta - 3 = 0$

(j) $\sin \theta = \operatorname{cosec} \theta$

(k) $\tan 2\theta = \sqrt{3}$

(l) $\sin 3\theta = \frac{1}{2}$

II

$\tan \theta = 0$

$\tan \theta = 1$

$\sec \theta = \sqrt{2}$

$\tan \theta = -1$

$\tan(\theta - 30^\circ) = -\sqrt{3}$

$\sqrt{3} \tan \theta - 1 = 0$

$\sin \theta = \sqrt{3} \cos \theta$

$4 \sin^2 \theta = 1$

$9 \sec^2 \theta = 16$

$3 \tan \theta = \cot \theta$

$2 \sin 2\theta - \sqrt{2} = 0$

$\sin^2 2\theta = \frac{3}{4}$

2. (a) If $\sin \theta = \frac{3}{5}$ and $\cos \theta > 0$, find $\cos \theta$ and $\tan \theta$.
- (b) If $\sin \theta = \frac{-4}{5}$ and $\cos \theta < 0$, find $\cos \theta$ and $\tan \theta$.
- (c) If $\tan \theta = \frac{-5}{12}$ and $\sin \theta > 0$, find $\sin \theta$ and $\cos \theta$.
- (d) If $\cos \theta = \frac{3}{4}$ and $\tan \theta < 0$, find the exact values of $\sin \theta$, $\tan \theta$ and $\operatorname{cosec} \theta$.
- (e) If $\tan \theta = 3$ and $\sin \theta > 0$, find the exact value of $\sin \theta$.

3. Find the non-negative values of θ not greater than 360° that satisfy the following equations.

(a) $\cos^2 \theta = \frac{1}{2}$

(b) $\sin^2 \frac{x}{2} = \frac{1}{4}$

4. Solve these equations for θ if $0^\circ \leq \theta < 360^\circ$.

(a) $\sin \theta = \frac{-\sqrt{3}}{2}$

(b) $\tan \frac{\theta}{2} = 2 \sin \frac{\theta}{2}$